

Forward to Geometrical Optics Presentation

Before embarking on a purely geometric approach to ophthalmic optics, I'd like to establish the benefit of this approach with an example problem. I will outline a geometric method of locating a tangential image point from refraction at a plane surface using known triangles to solve for unknown triangles. I expect this will be obviously more accessible to the average ophthalmic optics student than mathematics involving multivariable equations.

Wavefronts turn when one side is slowed more than the other, as would happen if one of your car's front wheels would brake harder than the other. This is best observed at the beach, where wavefronts from all directions bend, (refract), more parallel to the beach, no matter what direction they might have been traveling in the open ocean.

Wavefront G_0N_0 bends, (refracts), into wavefront GN along diameter G_0N when it travels G_0G in the same time it travels N_0N .

As $G_0 \Rightarrow N$, $G_0G \Rightarrow NK$,

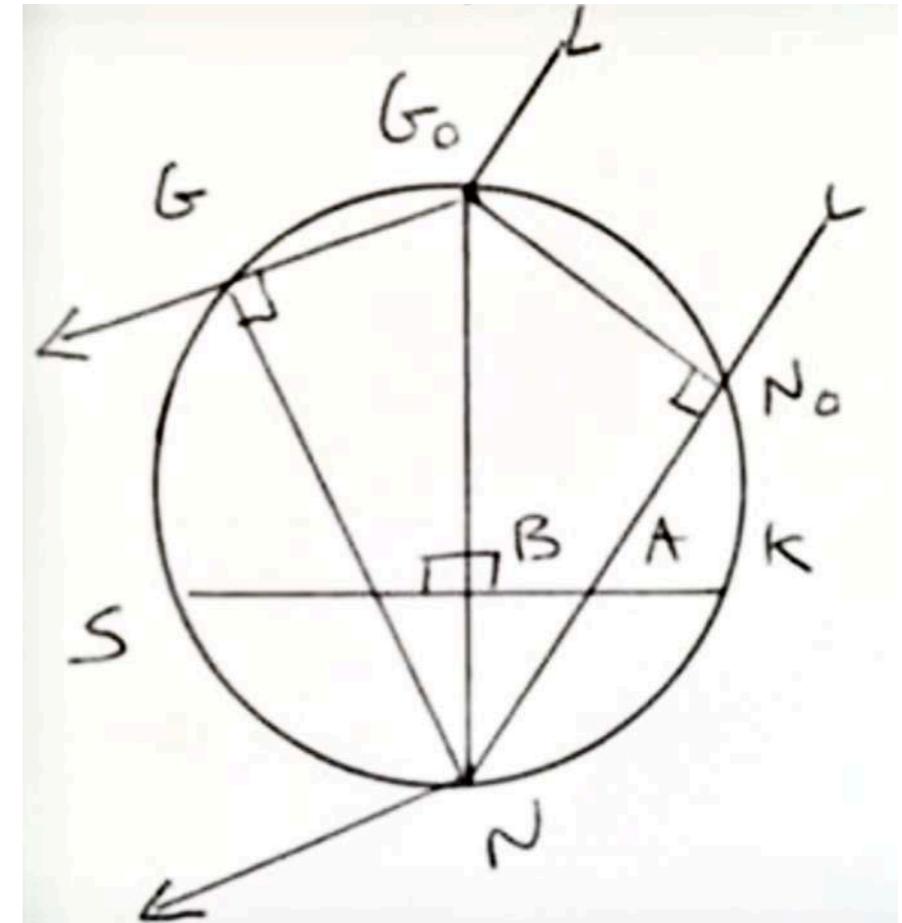
Therefore, let $G_0G = NK$.

Since equal arcs $\sim SN$ and $\sim KN$ subtend equal angles,

$\Delta N_0NK \cong \Delta KNA$, and:

$$\mathbb{R} = NN_0/GG_0 = NN_0/NK = NK/NA$$

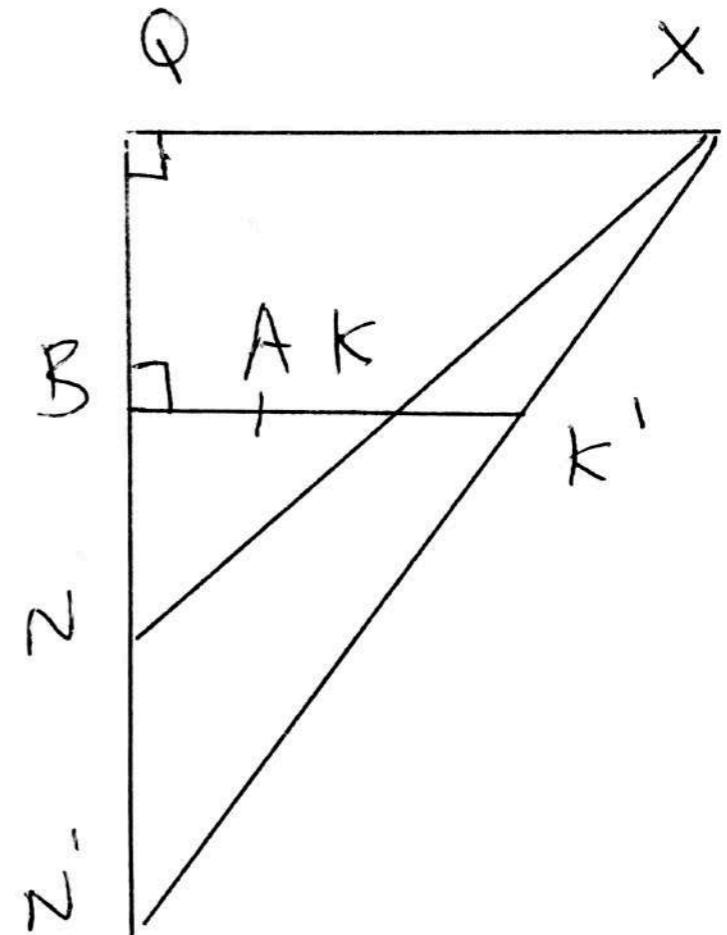
\mathbb{R} , the index of refraction, is therefore a velocity ratio.



Think of light traveling along an object and image ray as a wave, much like the sound wave traveling from a speaker to a listener. If sound waves reflect off an irregular surface, so that each travels a different distance to the listener, the result is garbled, and unintelligible. However, if a large enough quantity of reflected sound waves travel an equal distance, (at the same speed and thus take the same time), they arrive, “in phase,” and can be understood. They are then, “focused.”

The same would be true if some of the sound waves slowed down, and traveled a proportionately shorter distance; or sped up, and traveled a proportionately longer distance. These waves would be refracted, rather than reflected, and would still be, “focused,” since the speaker could be understood. The information they carried would be, “in phase.”

Section two of this material shows that only *two* object rays from point A can be refracted along a tangential section QBN of a plane surface and projected backwards *as if* to come from a single point X. Unless they are superimposed, they will be out of focus at X because the information they carry will be out of phase.

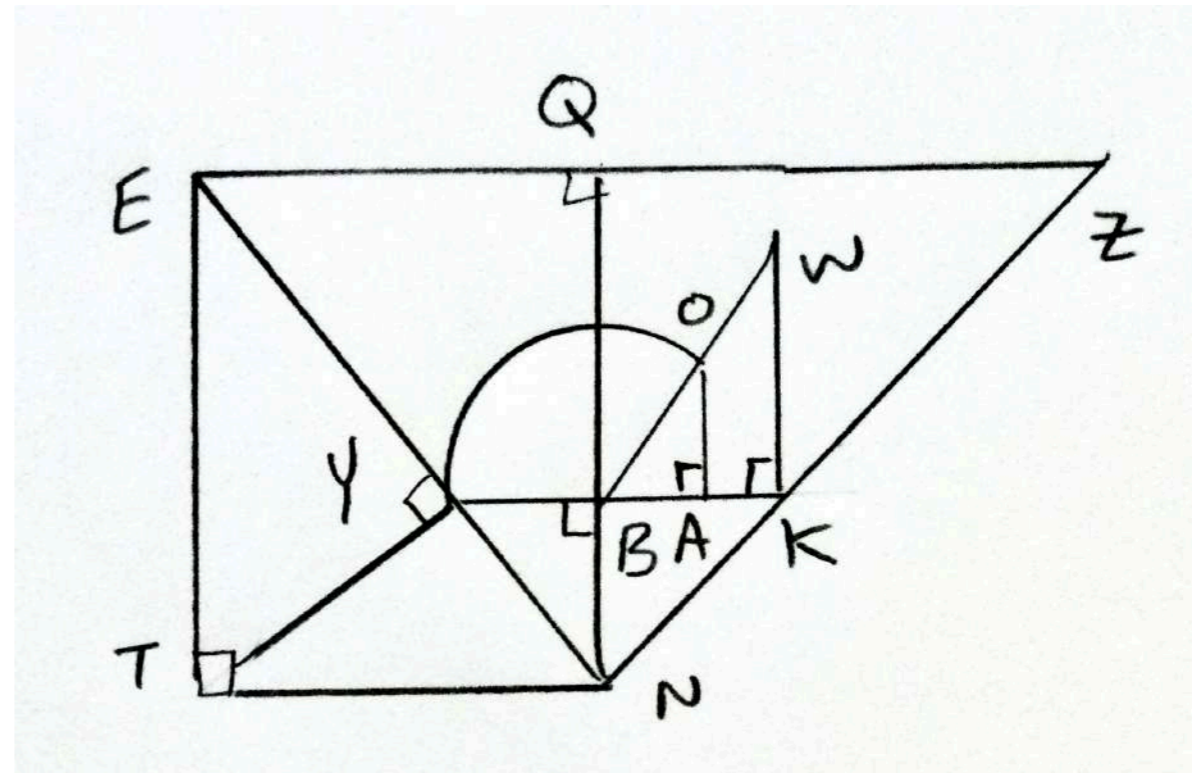


Section two also shows that these two rays are superimposed when this tangential template can be drawn with these conditions:

$$\mathbb{R} = NK/NA = OB/OA,$$

and $WK = YN$.

Under these conditions, Z is therefore the (tangentially) focused image of A.



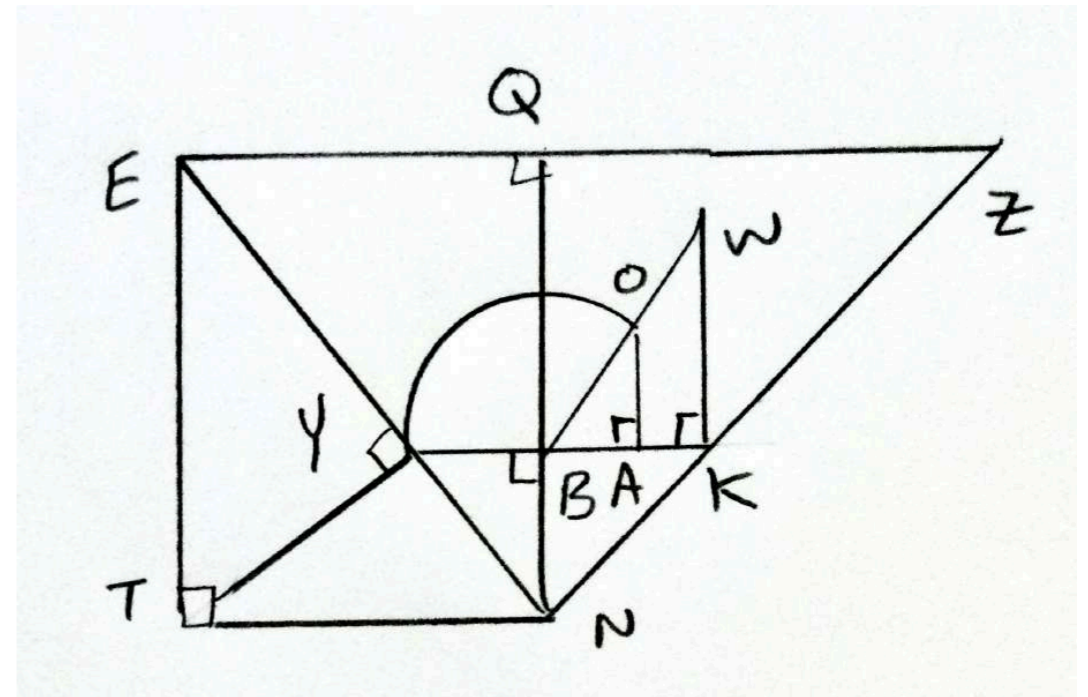
Unlike the tangential refraction just illustrated involving the bundle of rays around the object and image ray that vibrate in the plane represented by the given tangential template, sagittal refraction occurs involving the bundle of rays around the object and image ray that vibrate *perpendicular* to the given template. To visualize how a different sagittal focus and tangential focus can occur along the same image ray, consider the common bellows. Its sides can be compressed an equal or unequal angular amount, and still force air in the same direction, (though with different force).

The bundle of rays vibrating perpendicular to the given template involve equal angles of incidence to the refraction plane, given equal and opposite angular deviations from the object ray.

The bundle of rays vibrating in the given template involve unequal angles of incidence with the refraction plane given equal and opposite angular deviations from the object ray.

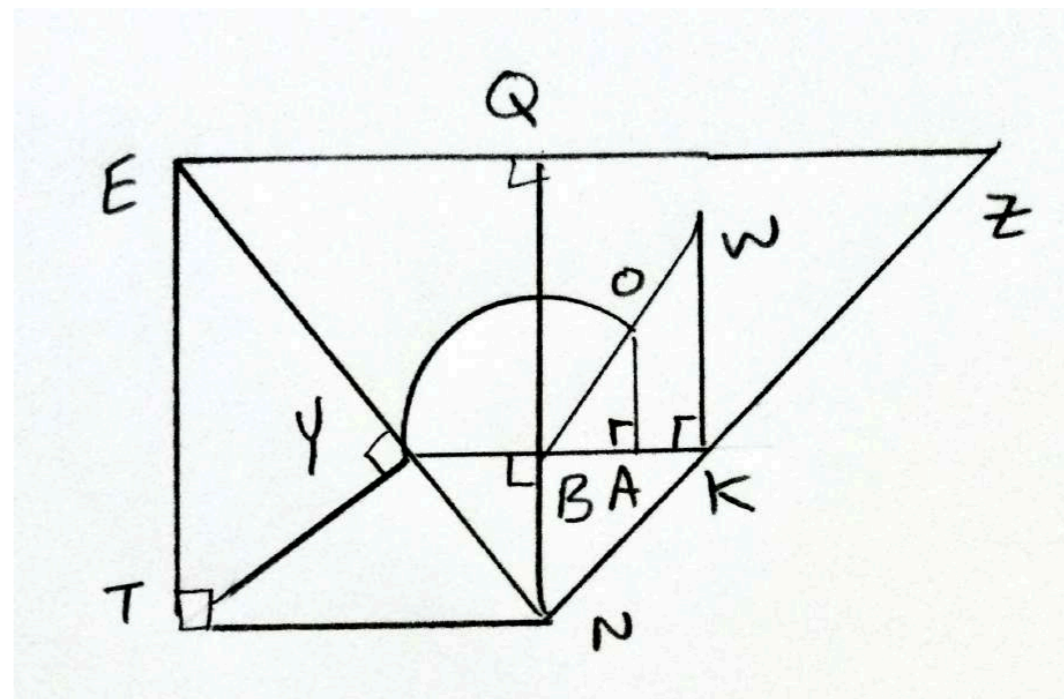
The tangential template allows for an understanding of how each variable of the problem affects others, as well as what is and what is not possible to discover with given variables.

For example, given an object distance AB and \mathbb{R} , we can construct $\triangle BAO$ by making:
 $\mathbb{R} = OB/OA$.

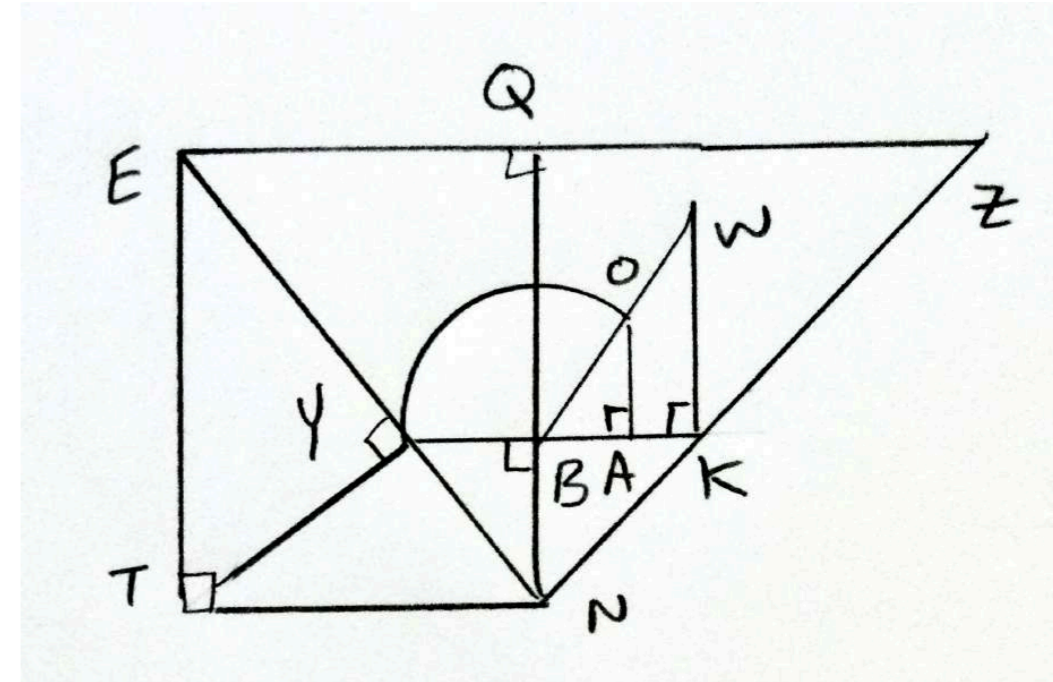


With $\triangle BAO$,
we can find BY by making
 $BO = BY$.

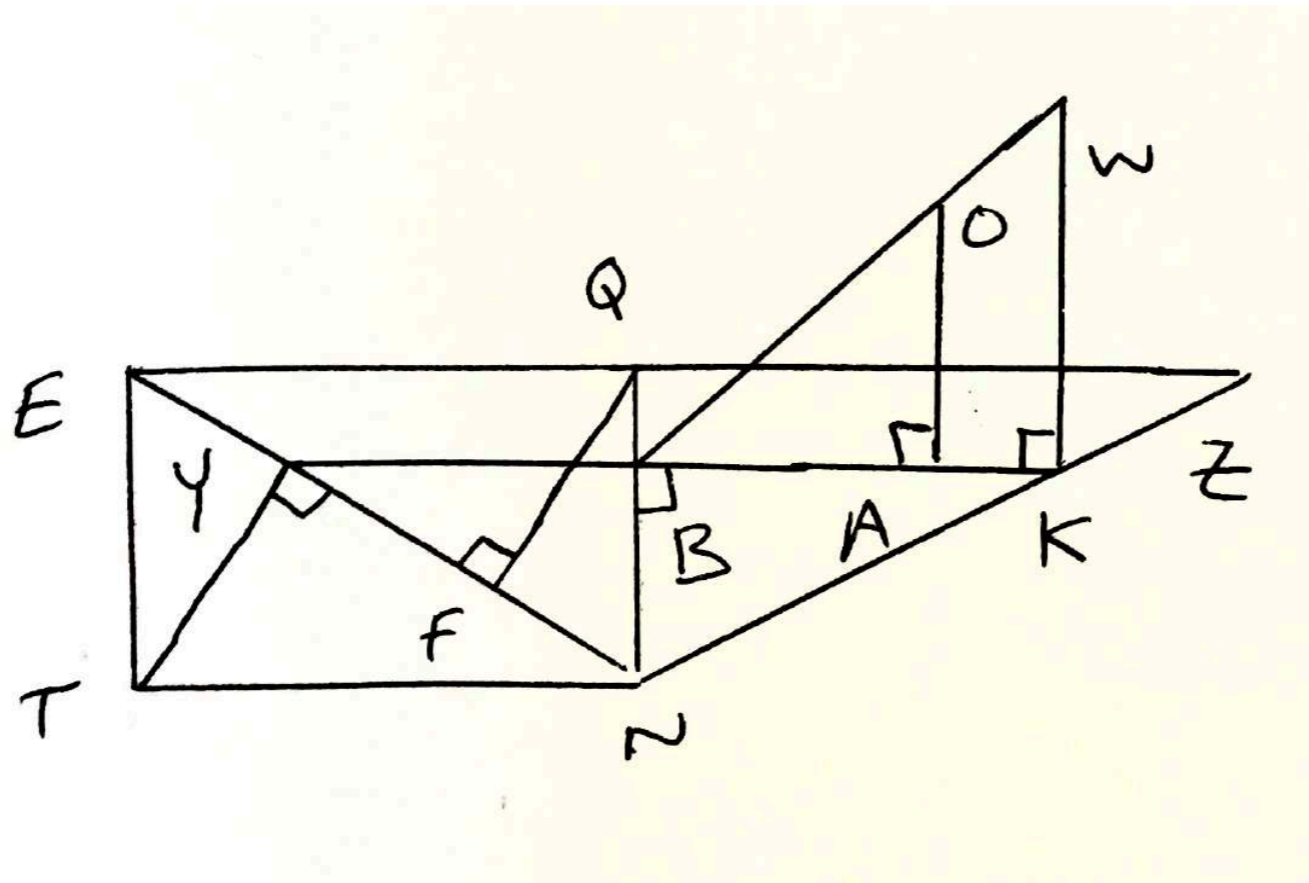
1). For a desired K , we can
use $\triangle BKW$ to find $\triangle BNY$ by
making $KW = YN$, and then
find $\triangle ZEN$ by first finding
right triangles $\triangle NYT$ and
 $\triangle TYE$.



2). For a desired N , we can use $\triangle BNY$ to find $\triangle BKW$ by making $YN = KW$, and then find $\triangle ZEN$ by first finding right triangles $\triangle NYT$ and $\triangle TYE$.

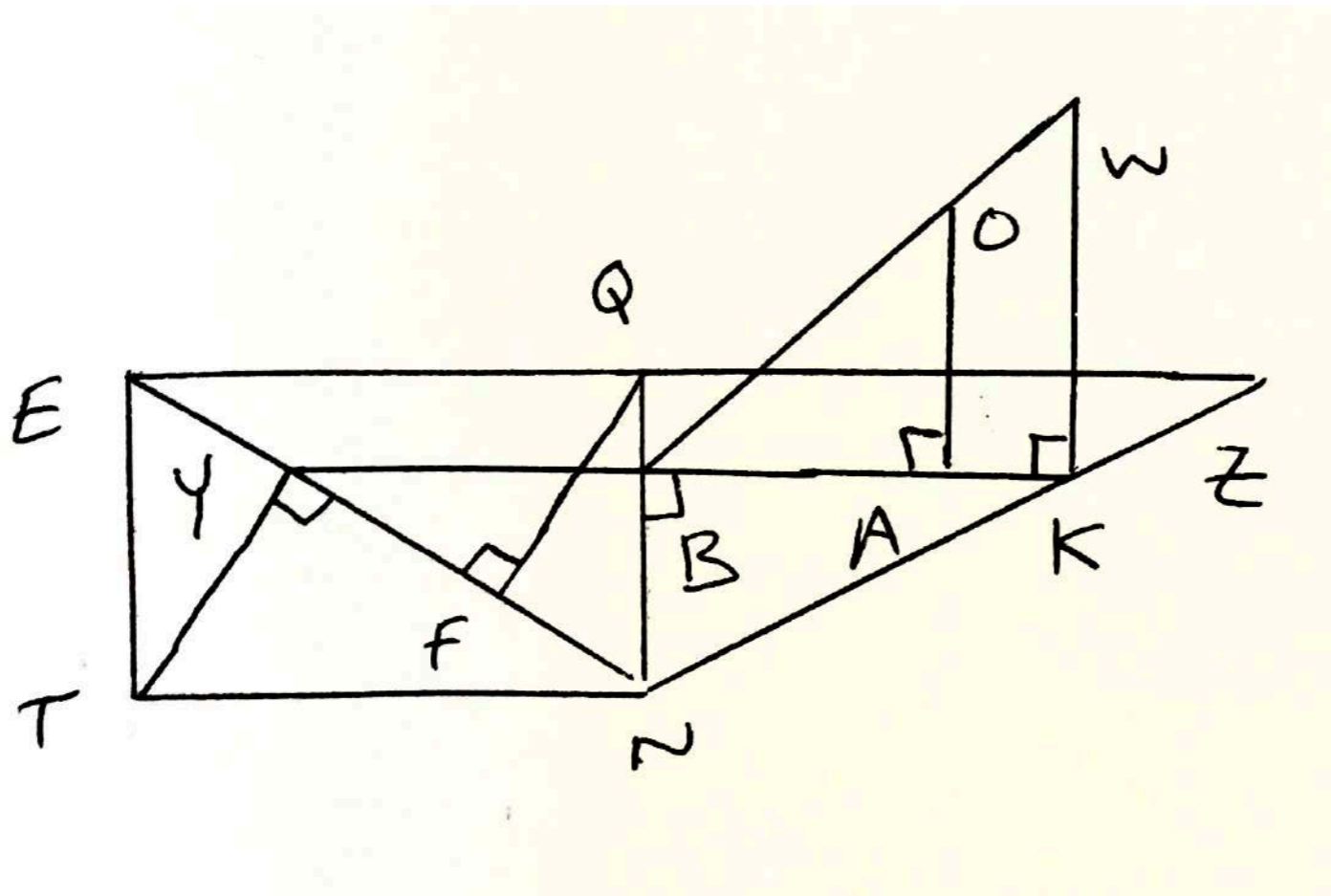


This template works when $YE > YN$, as shown previously; or when $YN > YE$, as shown here:



$$(\mathbb{R} = NK/NA = OB/OA; BO = BY; YN = KW)$$

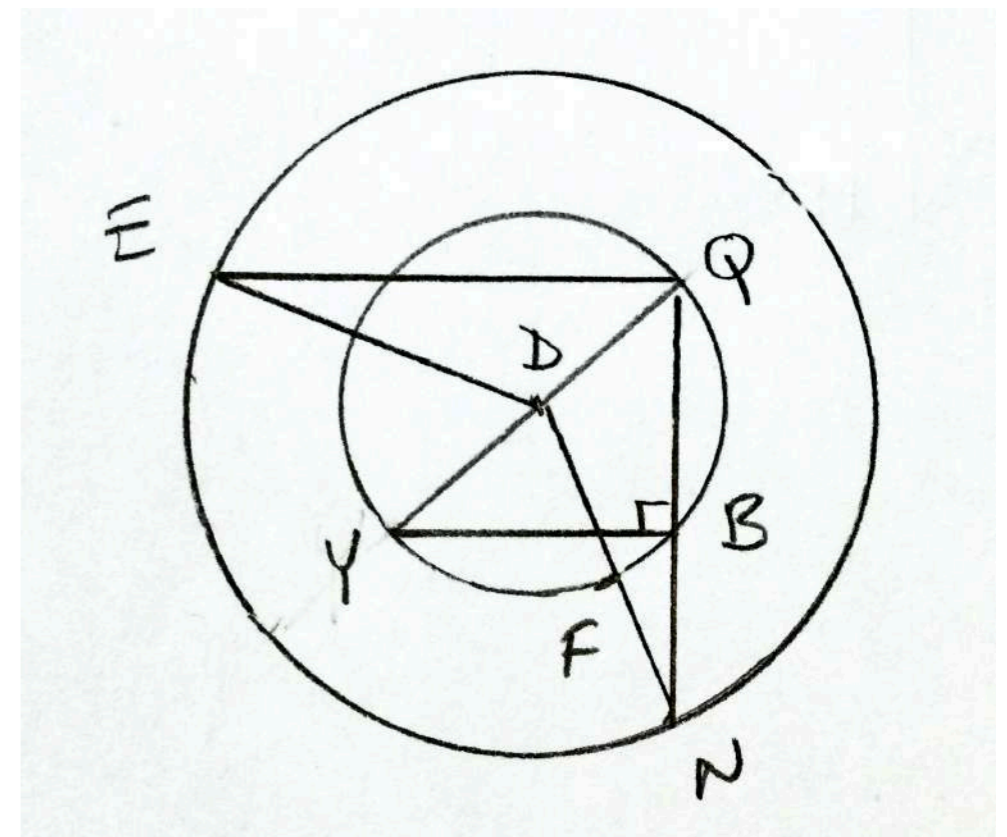
3). Using the template where $YN > YE$ as the example, for a desired Z , we can use ΔQBY to find ΔBNY .



$$(\mathbb{R} = NK/NA = OB/OA; BO = BY; YN = KW)$$

A concentric circle around circle $\odot QBY$ is drawn with its center at the midpoint of hypotenuse YQ , so that line segment YF lies on chord EN .

The arc intercepted by $\angle DEN$ equals that intercepted by $\angle DNE$.
Therefore, $\angle DEY = \angle DNF$.



$$DY = DF$$

$$DE = DN$$

$$\triangle EDY = \triangle NDF$$

$$EY = NF$$

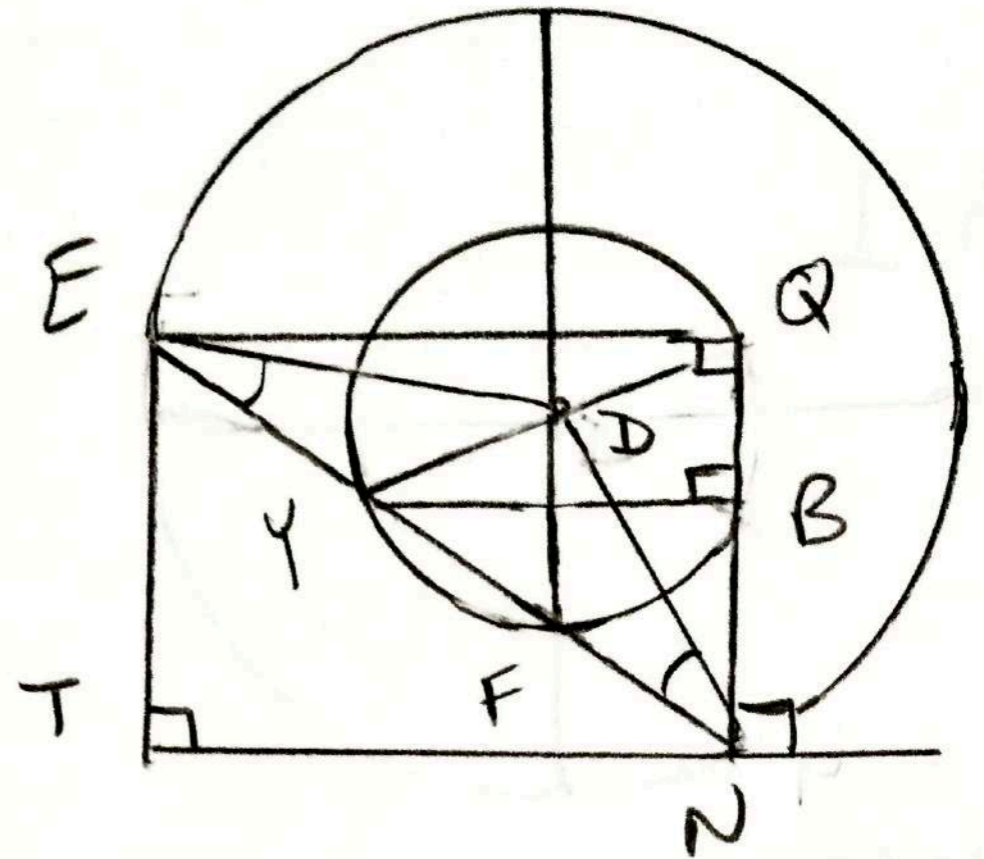
Since QY is a diameter,
 $\angle QFY$ is a right angle.

This means $\angle QFN$ is

also a right angle,

and since $EY = NF$,

$\angle TYE$ is a right angle.



Note that QZ varies with EN because:
 $QZ/EN = KB/YN = KB/KW = AB/AO$,
 which is a constant determined by \mathbb{R} .
 Therefore, \mathbb{R} , which determines image ray
 projection NK given AN, also determines the
 location of the focused tangential image along NK.

